Linear and Binary Search



Worksheet 1

Question 1

A librarian wants to implement a search algorithm to help locate a specific page number in a book. The figure below shows an example list of page numbers:

	[9, 15, 22, 24, 30, 40, 92]	
(a)	Using the figure above, explain how linear search would search for the integer 30.	
		
		[4 marks]
(b)	What property of the example of the page numbers above means the librarian could use a binary search algorithm?	
		(1)
(c)	The librarian knows that a binary search algorithm is more efficient than a linear search algorithm. Explain why the efficiency of these two algorithms is not an important factor when choosing what algorithm to implement for the page numbers in the figure above.	
		(2)

(Total 7 marks)

Question 2

The fruits shown below are organized in alphabetical order:

Apple	Banana	Cherry	Date	Elderberry	Fig	Grape	Honeydew	Jackfruit	Kiwi	Lemon	Mango	Nectarine	
(a) A I	oinary se	earch is	cond	ucted to fi	nd th	ne fruit	Lemon. W	hich fruit	s will k	oe exan	nined?		
(b) A I	oinary se	earch is	done	to locate	the f	ruit Gra	ape. Which	n fruits wi	ll be e	xamine	d?		[4 marks]
													[1 mark]
	Il more t		ee att	empts be	requ	ired to	identify an	y fruit? If	yes, v	which fr	uit(s)?	How many	/ fruits need
													[4 marks]

Question 3

The algorithm below is the binary search algorithm designed to search for a value within an array.

```
Line numbers are included but are not part of the algorithm.
For this algorithm, array indexing starts at 1.
    val ← 43
     arr ← [3, 5, 13, 43, 655, 872]
    left ← 1
    right ← LENGTH(arr)
5 WHILE left ≠ right
6
       mid ← (left + right) DIV 2
    IF val ≤ arr[mid] THEN
8
         right ← mid
9
       ELSE
10
          left \leftarrow mid + 1
11
        ENDIF
12
      ENDWHILE
```

(a) Complete the trace table for the algorithm above (you may not need to use all of the rows in the table). The final value of left is already given.

val	left	right	mid	arr[mid]
	4			

(5)

(b) Why would the binary search algorithm shown above not work when the array arr contains

(1)

(c)	on line 5 of the algorithm shown thm.	
	Shade one lozenge to show which of the following lines coabove as it would change the functionality of the algorithm	<u> </u>
	New Line 5	
	A WHILE left < right	
	${f B}$ WHILE NOT (left = right)	
	${f C}$ WHILE left < right AND left > right	
	${f D}$ WHILE left < right OR left > right	
		(1)
(d)	The final value of left in the algorithm above is 4. A program value to check whether val has been found or not in the algorithm.	•
	The programmer wants to extend the algorithm and introdutrue when the value has been found in the array or false	
	Write the pseudo-code or draw the flowchart that is needed the algorithm finishes, the new variable found is: true when val is found in arr false when val is not found in arr	to extend the algorithm so that when
	This code should follow on from the end of the algorithm a	above.
		(4)
		(Total 11 marks)